## SECOND SEMESTER (CUCBCSS—UG) DEGREE EXAMINATION, MAY 2019

B.C.A.<br>BCA 2C 03-COMPUTER ORIENTED STATISTICAL METHODS

(2014 Admissions)
Time : Three Hours
Maximum : 80 Marks

Part A<br>Answer all questions.<br>Each question carries 1 mark.

1. Sum of deviations observations from their arithmetic mean is $\qquad$
2. is theraphical method studying dispersion.
3. Set of all possible outcomes of a random experiment is known as

4. Three unbiased coins are tossedis thaprobability of getting at least one head.
5. Two random variables are said to be independent if $f(x, y)=$ $\qquad$
6. A distribution for which mean is greater than variance is $\qquad$
7. Standard deviation of sampling distribution of a statistic is called $\qquad$
8. The square of Standard. Normal distribution is $\qquad$
9. The joint distribution of sample observations is called $\qquad$
10. If $t_{\mathrm{r}}$ is consistent for $0, \mathrm{t}_{\mathrm{n}}{ }^{2}$ is consistent. for

$$
(10 \times 1=10 \text { marks })
$$

## Part B (Short Answer Type Questions)

Answer all questions.
Each question carries 2 marks.
11. For any two positive numbers, prove that $\mathrm{AH}=\mathrm{G}^{2}$, where A is the arithmetic mean, G is the geometric mean, and H is the harmonic mean.
12. Give classical definition of probability.
13. Define random variable and give two examples.
14. Define F-statistiL
15. What is a mean by a statistical hypothesis? Explain simple and composite hypothesis.

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\text { (5 x } 2=10 \text { marks })
$$

## Part C (Short Essay Type Questions)

Answer any five questions.
Each question carries 4 marks,
16. Explain the method of constructing a Lorenz curve.
17. Prove that standard deviation is independent of change of origin, but not of scale.
18. Let $\mathrm{B} \mathrm{c}_{-} \mathrm{A}$, prove that (i) $\mathrm{P}\left(\mathrm{A} n B^{c}\right)=\mathrm{P}(\mathrm{A}) \mathrm{P}(\mathrm{B})$; and (ii) P (B) $\mathrm{P}(\mathrm{A})$.
19. The p.d.f, of a random variable X is given by $f(x)=k x(1-x) ; O<x 1$ :
(i) Find the value of $k$.
(ii) Obtain the distribution function of X .
20. Define the moment generating function of a random variable. Explain how you will obtain moments from a moment generating function.
21. Obtain the sampling distribution of mean of the samples from a Normal population.
22. Obtain the interval estimate of variance of a Normal population.
23. Obtain the maximum likelihood estimator of parameter of a Poisson population.

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\text { (5 x } 4=20 \text { marks })
$$

> Part D (Essay Questions)
> Answer any five questions.
> Each question carries 8 marks.
24. Obtain the co-efficient variation for following data :
Length of life (in hours) : 500-700
L 700--900
No.of bulbs
25. Fit a straight line to the following data:

| Year | 1992 | 1994 | 1996 | 1998 | 2000 | 2002 | 2004 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| Production | 77 | 81 | 88 | 94 | 94 | 96 | 98 |

26. Find the co-efficient of correlation between $X$ and $Y$ from the following data :

| 15.5 | 16.5 | 17.5 | 18.5 | 19.5 | 20.5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 75 | 60 | 50 | 50 | 45 | 40 |

27. The two lines of regression are given by $8 x-10 y-4-66=0$ and $40 x-18 y=214$ :
(a) Identify the regression lines.
(b) Find the mean values of X and Y .
(c) Find the correlation co-efficient between X and Y .
(d) Find the standard deviation of Y , if the standard deviation of X is 3 .
28. From a group of 3 Indians, 4 Pakistanis and 5 Americans, a sub-committee of four peoples is selected by lots. Find the probabilities that the sub-committee will consist of :
(a) 2 Indians and 2 Pakistanis.
(b) 1 Indian, 1 Pakistani and 2 Americans.
(c) At least one Indian.
29. A random variable $X$ has the p.m.f. given by :

| X | $-\mathbf{3}$ | $\mathbf{- 1}$ | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{x})$ | $k^{2}$ | $2 \mathrm{k}^{2}+k$ | $2 \mathrm{k}^{2}+3 \mathrm{k}$ | $4 \mathrm{k}^{2}+5 \mathrm{k}$ | $3 \mathrm{k}^{2}+3 \mathrm{k}$ | $2 \mathrm{k}^{2}+k$ |

(a) Find the value of $k$.
(b) Obtain the distribution function of X
(c) Find $P(X>1)$ and $P(X 52)$.
30. From a Normal population $\mathrm{N} \mathbf{S}^{2}$ ), obtain :
(a) The MLE of p when $6^{2}$ is known.
(b) The MLE of $0^{2}$ when $\mu$ is known.
31. Let $x_{1}, x_{2}, \ldots, x_{9}$ is a random sample of size nine taken from a Normal population $N$ 25). To test $H_{o}: \mu=5$ against $H_{1}: p,=6$, the critical region suggested is 7 where $x$ is the sample mean. Find the significant level and power of the test.

