	D	7	3	<b>2</b>	8	8
--	---	---	---	----------	---	---

(Pages: 3)

Nam	<del>C</del>
Reg.	No

# FIRST SEMESTER B.A./B.Sc. DEGREE EXAMINATION, NOVEMBER 2019

(CBCSS-UG)

Mathematics

## MTS 1C 01-MATHEMATICS-I

(2019 Admissions)

Time: Two Hours

Maximum: 60 Marks

#### Section A

Answer any number of questions.

Each question carries 2 marks.

Maximum Marks 20.

- 1. Find the derivative of  $f(x) = 3x^2 + 8x$  at  $x_0 = -2$  and  $x_0 = \frac{1}{2}$ .
- 2. A rock thrown down from a bridge has fallen  $4t + 4.9t^2$  meter after t seconds. Find its velocity at t = 3.
- 3. Find  $\lim_{x \to \infty} \frac{5x^2 3x + 2}{x^2 + 1}$ .
- 4. Suppose that  $f(t) = \frac{1}{4}t^2 t + 2$  denotes the position of a bus at time t. Find the acceleration.
- 5. A bagel factory produces  $30x 2x^2 2$  dollars worth of bagels for each x worker hours of labour. Find the marginal productivity when 5 worker hours are employed.
- 6. The velocity of a particle moving along a line is 3t + 5 at time t. At time 1, the particle is at position 4. Where is at time 10?
- 7. Use the second derivative test to analyze the critical points of the function  $f(x) = x^3 6x^2 + 10$ .

Turn over

- 8. Find inflection point of the function  $f(x) = x^2 + \frac{1}{x}$ .
- 9. Find  $\lim_{x\to 0^+} x \ln x$ .
- 10. Draw the graph of the step function g on [0,1] defined by  $g(x) = \begin{cases} -2, & \text{if } 0 \le x < \frac{1}{3} \\ 3, & \text{if } \frac{1}{3} \le x \le \frac{3}{4}. \end{cases}$  Compute the signed area of the region between its graph and the x-axis.
- 11. Find the sum of the first n integers.
- 12. Find  $\int_0^4 \left( t^2 + 3t^{\frac{7}{2}} \right) dt$ .

#### Section B

Answer any number of questions.

Each question carries 5 marks.

Maximum Marks 30.

- 13. (a) Differentiate  $\frac{1}{(x^3+3)(x^2+4)}$ .
  - (b) Calculate approximate value for  $\sqrt{8}$  using the linear approximation around  $x_0 = 9$ .
- 14. Find the equation of the tangent line to the curve  $2x^6 + y^4 = 9xy$  at the point (1, 2).
- 15. Water is flowing into a tub at  $3t + \frac{1}{(t+1)^2}$  gallons per minute after t minutes. How much water is in the tub after 2 minutes if it started out empty.
- 16. State mean value theorem. Let  $f(x) = \sqrt{x^3 8}$ . Show that somewhere between 2 and 3 the tangent line to graph of f has slope  $\sqrt{19}$ .

- 17. Find the dimensions of a box of minimum cost if the manufacturing costs are 10 cents per square meter on the bottom, 5 cents per square meter on the sides, and 7 cents per square meter on the top. The volume is to be 2 cubic metres and height is to be 1 metre.
- 18. The region between the graph of  $x^2$  on [0,1] is revolved about the x-axis. Sketch the resulting solid and find its volume.
- 19. Find the area between the graphs of  $y = x^3$  and  $y = 3x^2 2x$  between x = 0 and x = 2.

### Section C

Answer any one question.

Each question carries 10 marks.

Maximum Marks 10.

20. (a) Differentiate 
$$\frac{x^{\frac{1}{2}} + x^{\frac{3}{2}}}{x^{\frac{3}{2}} + 1}$$
.

(b) Find inflection point of the function  $f(x) = x^2 + \frac{1}{x}$ .

21. (a) Find 
$$\lim_{x\to 0} \left( \frac{1}{x \sin x} - \frac{1}{x^2} \right)$$
.

(b) Find average value of  $f(x) = x^2 \sin x^3$  on  $[0, \pi]$ .