

## FIRST SEMESTER B.C.A. DEGREE EXAMINATION, JANUARY 2013

(CCSS)

BCA

CA 10 02—DISCRETE MATHEMATICS

Time : Three Hours \_\_\_\_\_

Maximum : 30 Weightage

## Part A (Objective Type Questions)

*Answer all twelve questions.*1. The value of  $c(n, n)$  is :

(a) 1.

(b)  $n$ .

(c) 0.

(d)  $n!$ .2. What is the order of the recurrence relation  $a_r - 6a_{r-1} = 0, r \geq 1$ .

(a) 0.

(b) 1.

(c) 2. \_\_\_\_\_

(d) 6.

3. Example of a group of four elements.

(a)  $S_4$ .

(b) Klein group.

(c) Set of integers less than under addition.

(d)  $Z_4$  under multiplication.4. The value of  $nP_{n-1}$  is :(a)  $n$ .(b)  $n!$ .

(c) 1.

(d)  $n-1$ .5. If  $p = F$  and  $q = F$  then  $p \vee q$  is \_\_\_\_\_6. The negation of  $\neg p \vee q$  is \_\_\_\_\_7. The value of  $01$  is \_\_\_\_\_8. Formula for  $p(n, r)$  is \_\_\_\_\_9. If  $p = T$  then  $p \wedge \neg p = F$ . True or False.

10. Can every group of prime order a generator ?

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11. Every integral domain is a field. True or False.

12.  $c(n, r) = c(n, n - r)$ . True or False.

(12 x 1 = 12 weightage)

### Part B (Short Answer Questions)

Answer all questions.

13. Form the conjunction of :

P : It is raining today.

Q : There are 20 tables in this room.

14. Evaluate  $p(n, r)$  for  $n = 6$  and  $r = 2$ .

15. Find the number of ways to paint 12 offices so that 3 of them will be green, 2 of them pink, 2 of them yellow and the **remainings** are white.

16. If  $c(n, 9) = c(n, 8)$ . Then find  $c$

17. Define commutative ring with example.

18. Write the truth table for conjunction and disjunction.

19. Symbolize the expression

"all the world loves a lover".

20. Suppose a housekeeper wants to schedule spaghetti dinner three times each week. Find the number of ways of scheduling it.

21. If  $G$  is group with binary operation  $*$  and if  $a$  and  $b$  are any elements of  $G$ . Then show that the linear equation  $a * x = b$  and  $y * a = b$  have unique solutions in  $G$ .

(9 x 1 = 9 weightage)

### Part C (Short Essay Questions)

Answer any five questions.

If  $a = a_0 + a_1r + a_2r^2 + \dots + a_nr^n$ , show that  $a = o(r^n)$ .

If  $\frac{1}{8!} + \frac{1}{9!} = \frac{x}{10!}$  find  $x$ .

Find the value of  $n$  such that  $p(n, 5) = 42 p(n, 3)$ .

Show that every field  $F$  is an integral domain.

State and prove division algorithm for  $\mathbb{Z}$ .

27. Find the truth table for  $(p \vee Q) \vee p$ .

28. Let  $a = r + O(1/r)$  and  $b = \sqrt{r} + O(1/r)$ . Show that  $ab = r^{3/2} + O(r^{1/2})$ .

(5 x 2 = 10 weightage)

### Part D (Essay Questions)

Answer any two questions.

29. Solve the equations :

$$a_r = 3a_{r-1} + 2b_{r-1} \text{ and}$$

$$b_r = a_r + b_{r-1} \text{ with the}$$

boundary conditions  $a_0 = 1$  and  $b_0 = 0$ .

30. If  $\mathbf{R}$  is a ring with additive identity 0, then for any  $a, b \in \mathbf{R}$ , we have

(a)  $0 \cdot a = a \cdot 0 = 0$ .

(b)  $a(-b) = (-a)b = -(ab)$ .

(c)  $(-a)(-b) = ab$ .

31. Write the truth table for  $\sim(p \wedge Q)$  and  $(\sim p \vee Q)$  and verify them.

(2 x 4 = 8 weightage)