

THIRD SEMESTER **B.C.A.** DEGREE EXAMINATION, NOVEMBER 2014

(U.G.—CCSS)

Complementary Course

CA 3C 06—OPERATIONS RESEARCH

Time : Three Hours

Maximum : 30 Weightage

Part A

*Answer all questions.***(Weightage 1 for bunch of 4)**

1. A physical model is an example of :

- (a) Iconic model.
- (b) Analogue model.
- (c) Verbal model.
- (d) Symbolic model.

2. Minimization of objective function in **LPP** means :

- (a) Least value chosen among the allowable decisions.
- (b) Greatest value chosen among the allowable decisions.
- (c) Both (a) and (b).
- (d) None of the above.

3. For maximization **LPP**, the objective function coefficient for an artificial variable is :

- (a) + M.
- (b) — M.
- (c) + 1.
- (d) Zero.

4. The dual of the primal maximization **LPP** having m constraints and n non negative variables should :

- (a) A minimization **LPP**
- (b) Have n constraints and m non-negative variables.
- (c) Both (a) and (b).
- (d) None of the above.

5. While solving a transportation problem, the occurrence of degeneracy means that ?

- (a) Total supply equals total demand.
- (b) The solution so obtained is not feasible.
- (c) The few allocations become negative.
- (d) None of the above.

Turn over

6. The method used for solving an assignment problem is called :

- (a) **MODI** method.
- (b) Reduced matrix method.
- (c) Hungarian method.
- (d) None of the above.

7. Sequencing problems involving processing of two jobs on n machines :

- (a) Can be solved graphically.
- (b) Cannot be solved graphically.
- (c) Have a condition that the processing of two jobs must be in the same order.
- (d) None of the above.

8. In critical path analysis, **CPM** is :

- (a) Event oriented.
- (b) Probabilistic in nature.
- (c) Deterministic in nature.
- (d) Dynamic in nature.

9. A transportation problem can be represented as a network flow problem where :

- (a) Origins represent sinks and destinations the sources.
- (b) Origins represent sources and destinations the sinks.
- (c) Objective is to maximize the network flow.
- (d) Per unit transportation costs become irrelevant.

10. The problem of replacement is not concerned about the :

- (a) Items that deteriorate graphically.
- (b) Items that fail suddenly.
- (c) Determination of optimum replacement interval.
- (d) Maintenance of an item to work out profitability.

11. Inventories in general are build up to :

- (a) Satisfy demand during period of replenishment.
- (b) Carry reserve stocks to avoid shortages.
- (c) Keep pace with changing market conditions.
- (d) All of the above.

12. If **EOQ** is calculated, but an order is then placed which is smaller than this, will the total inventory cost :

- (a) Increase. (b) Decrease.
(c) Either increase or decrease. (d) No change.

(12 x 3 = 36 weightage)

Part B

Answer all questions.
(Weightage 1)

13. State the general linear programming problem in standard form.
14. Write the role of pivot element in simplex table.
15. Construct the dual of :

Maximize $2000x_1 + 3000x_2$

subject to $6x_1 + 9x_2 \leq 100$

$2x_1 + x_2 \leq 20$

$x_1, x_2 \geq 0$.

16. What is an unbalanced transportation problem ?
17. How do you interpret assignment problem as a linear programming model ?
18. What is meant by graphing in Network Analysis ?
19. What is no passing rule in a sequencing algorithm ?
20. What is a replacement problem ?
21. A certain item costs Rs. 235 per ton. The monthly requirement is 5 tons and each time the stock is replenished there is a set-up cost of Rs. 1000. The cost of carrying inventory has been estimated at 10% of the value of the stock per year. What is the optimal order quantity ?

(9 x 1 = 9 weightage)

Part C

Answer any five questions.
(Weightage 2)

22. An animal feed company must produce 200 lbs of a mixture containing the ingredients X_1 and X_2 . X_1 costs Rs. 3 per lb. and X_2 costs Rs. 3 per lb. Not more than 80 lbs. of X_1 can be used and minimum quantity to be used for X_2 is 60 lbs. Find how much of each ingredient should be used if the company wants to minimize the cost. Formulate the **LPP**.

Turn over

23. Use dual simplex method to solve :

$$\text{Minimize } Z = 10x_1 + 6x_2 + 2x_3$$

subject to

$$-x_1 + x_2 + x_3 \geq 1$$

$$3x_1 + x_2 - x_3 \geq 2$$

$$x_1, x_2, x_3 \geq 0$$

24. Solve the following assignment problem :-

	1	2	3	4
A	5	8	3	2
B	10	7	5	8
C	4	10	12	10
D	8	6	9	4

25. Find the optimal order quantity for a product for which the price breaks are as follows :

Quantity	Purchasing Cost per unit (Rs.)
$0 < Q_1 < 100$	20.00
$100 \leq Q_2 < 200$	18.00
$200 < Q_3$	16.00

The monthly demand for the product is 400 units, the cost of storage is 20 % of the unit cost and ordering cost is Rs. 25.00 per month.

26. The purchase cost of a machine is Rs. 13,000 and its installation amount is Rs. 3,600. Its scarp value is Rs. 1600. The maintenance costs (in Rs.) found from experience are as follows :

Year	1	2	3	4	5	6	7
Maintenance cost	250	750	1000	1500	2100	2900	4000

When should the machine be replaced ?

27. A contractor has to supply 20,000 units per day. He can produce 30,000 units per day. The cost of holding a unit in stock is Rs. 3 per year and the set-up cost per run is Rs.50. How frequently and of what size the production runs be made.

28. Given the following information :

Activity	0 - 1	1 - 2	1 - 3	2 - 4	2 - 5	3 - 4	3 - 6	4 - 7	5 - 7	6 - 7
Duration	2	8	10	6	3	3	7	5	2	8

Draw the arrow diagram. Identify critical path and find the total project duration.

(5 x 2 = 10 weightage)

Part D

Answer any two questions.

(Weightage 4)

29. Use two-phase method to :

$$\text{Maximize } Z = 3x_1 - x_2$$

subject to

$$2x_1 + x_2 \geq$$

$$x_1 + 3x_2 \geq$$

$$x_2 \leq 4$$

$$x_1, x_2 \geq 0.$$

30. Solve the following transportation problem :

To

From

	A	B	C	D	Available
I	21	16	25	13	11
II	17	18	14	23	13
III	32	27	18	41	19
Requirement	6	10	12	15	43

31. Table below shows jobs, their normal time and cost and crash time and cost for a project :

Job	Normal time	Cost	Crash time	Cost (Rs.)
1 - 2	6	1400	4	1900
1 - 3	8	2000	5	2800
2 - 3	4	1100	2	1500

Turn over

<i>Job</i>	<i>Normal time</i>	<i>Cost</i>	<i>Crash time</i>	<i>Cost (Rs.)</i>
2 - 4	3	800	2	1400
3 - 4	Dummy			
3 - 5	6	900	3	1600
4 - 6	10	2500	6	3500
5 - 6	3	500	2	800

Indirect cost for the project is Rs. 300 per day :

- (i) Draw the network of the project.
- (ii) What is the normal duration cost of the project.
- (iii) If all activities are crashed, what will be the project duration and corresponding cost ?
(2 x 4 = 8 weightage)