

**D 12499**

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Name.....

Reg. No.....

**FIRST SEMESTER M.Sc. DEGREE EXAMINATION, JANUARY 2006**

Computer Science

CS 104. NUMERICAL METHODS

(2004 and earlier admissions)

Time : Three Hours

Maximum : 60 Marks

**Part A**

*Answer any five questions.  
Each question carries 3 marks.*

1. Define Relative error and Percentage error.
2. Find the root of the equation  $xe^x - 3 = 0$ , that lies between 1 and 2, correct to four places of decimals, using the method of false position.
3. Find the smallest positive root of the equation  $3x^3 - 9x^2 + 8 = 0$ , correct to four places of decimals using **Newton-Raphson** method.
4. Find the inverse of the given matrix by Gauss elimination method :

$$\begin{bmatrix} 4 & 1 & 2 \\ 2 & 3 & -1 \\ 1 & -2 & 2 \end{bmatrix}$$

5. Determine the **Lagranges** method the percentage number of patients over 40 years, using the following data :—

|                            |     |    |    |    |
|----------------------------|-----|----|----|----|
| Age over (x) years         | 30  | 35 | 45 | 55 |
| % number (y) of patients : | 148 | 96 | 68 | 34 |

6. Evaluate  $\int_0^2 \log_e \sqrt{1+x} dx$ , using Simpson's one-third rule with 8 subintervals.
7. Using Taylor's series method of the fourth order, find y at x = 1.1 by solving the equation

$$\frac{dy}{dx} = x^2 + y^2 \text{ given } y(1) = 2.$$

(5 x 3 = 15 marks)

**Turn over**

## Part B

Answer any **three** questions.  
Each question carries **15** marks.

8. Solve the equation  $\frac{dy}{dx} = \frac{1}{x+y}$ ,  $y(0) = 1$  for  $y(0.1)$ , using **Runge-Kutta** method of the fourth order.

9. Find all the **eigenvalues** and **eigenvectors** of the matrix :

$$\begin{vmatrix} 2 & 3 & 1 \\ 3 & 2 & 2 \\ 1 & 2 & 1 \end{vmatrix}$$

10. Find the quadratic factor  $x^2 + px + q$  of the polynomial  $x^4 - 3x^3 + 20x^2 + 44x + 54$  using **Baird** method and taking the initial values of  $p$  and  $q$  as 2 and 2.

11. Obtain the relation of the form  $y = ab^x$  for the following data by the method of least squares

|       |     |      |      |      |       |
|-------|-----|------|------|------|-------|
| $x$ : | 2   | 3    | 4    | 5    | 6     |
| $y$ : | 8.3 | 15.4 | 33.1 | 65.2 | 127.4 |

(3 x 15 = 4k.)