

**FIRST SEMESTER M.Sc. DEGREE EXAMINATION, DECEMBER 2009****Computer Science (Main)****CS 101—DISCRETE MATHEMATICS****(2005 Admissions)**

Time : Three Hours

Maximum : 80 Marks

**Part A***Answer any **five** questions.*

1. State and prove De Morgan's law on sets.
2. Define equivalence of two formulas and prove the equivalence of following two formulas :  
 $(P \rightarrow Q), P \vee \sim Q$ .
3. State pigeonhole principle and its extension. Show that there are at least 6 different ways to choose 3 numbers from 1 to 10 so that all choices have the same sum.
4. Find the explicit formula for the recurrence relation  $x(n) = 4x(n-1) + 5x(n-2)$ ,  $x(1) = 3$ ,  $x(2) = 6$ .
5. (a) Show that  $[0, 1, 2, 3, 4]$  is a group under the operation " $\text{*mod}5$ ".  
 (b) Find the inverse of the permutation.  
 $(1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7)$   
 $(6 \ 1 \ 5 \ 7 \ 2 \ 4 \ 3)$
6. Define lattice. Let  $(L, \cdot, +)$  be a lattice in which  $\cdot$  and  $+$  denote meet and join respectively. Show that  $a \cdot b \Leftrightarrow a * b = a \Leftrightarrow a + b = b$ .
7. Identify a finite state machine that accepts strings over  $\{a, b\}$  that begins and ends with odd number of a's.

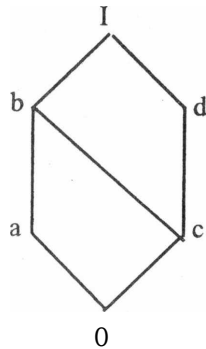
(5 x 8 = 40 marks)

**Part B***Answer any **four** questions.*

8. (a) Prove that  $\overline{\bigcup_i A_i} = \bigcap_i \overline{A_i}$ .
- (b) When is a function invertible? Give an example.

**Turn over**

9. (a) Define induction. Show that  $n^3 + 2n$  is divisible by 3.  
 (b) Write the explicit formula for Fibonacci number.
10. Define and give examples of group, subgroup, ring, coset, normal group, cyclic group, integral domain.
- 11 (a) Given the members of the poset as  $(1, 2), (2, 3), (3, 4), (1, 5), (5, 4), (9, 5), (5, 6), (6, 7), (8, 7)$ .  
 Draw Hasse diagram and find minimal and maximal elements.  
 (b) Verify if the Hasse diagram above is a Lattice.
12. (a) If  $P \rightarrow Q$  is false, find the truth value of  $\sim(\sim Q) \rightarrow Q$ .  
 (b) Define equivalence relation with an example. Find its partition.
13. (a) Verify distributive properties for the elements of the Lattice  $(A, \leq)$  as shown in the figure. Find the complement of  $a, b$ .



- (b) Discuss Hamming distance.

(4 x 10 = 40 marks)