Name.....

FL T SEMESTER M.Sc. DEGREE EXAMINATION, DECEMBER 2009

Computer Science (Main)

CS 104—THEORETICAL COMPUTER SCIENCE

(2005 Admissions)

Time : Three Hours

Maximum : 80 Marks

Part A

Answer any **five** questions.

- 1. Define a finite automata and its language. Give an example. Also find the regular expression.
- 2. State pumping lemma for regular sets. Show that $\{a^{i}b^{i} / i = 1\}$ is not regular.
- 3. Find the reduced CFG equivalent to S aS I AB, A $\mathbf{B} \to \mathbf{E}, \mathbf{D}$ b.
- 4. State pumping lemma for CFG and show that $\{a^{i}b^{i}c^{i} / i = 1\}$ is not CFL.
- 5. Define TM and describe ID. What is the language of the TM?
- 6. State and provide informal proof for Chomsky's hierarchy.
- 7. Find the disjunctive normal form of $(1 P \lor \neg Q)$ P n **R**).

 $(5 \ge 8 = 40 \text{ marks})$

Part B

Answer any **four** questions.

- 8. State Kleen's theorem and outline the proof.
- 9. Find the reduced state DFA that accepts $(0 + 11) 0^*1$.
- 10. Construct a CFG for the language $\{a^ib^i / i = 1\}$ and hence find a PDA.
- 11. Write a note on the halting problem in TM.
- 12. Discuss P, NP, NP-complete problems giving examples of each type.
- 13. (a) By constructing suitable universe of discourse show that 3x (P(x) = Q(x))

 $(3x P(x) \exists x Q(x))$ is not valid.

- (b) Show that the following arguments is valid.
 - (i) All men are mortal. (ii) Socrates is man.

(iii) So Socrates is mortal.

 $(4 \times 10 = 40 \text{ marks})$