

SECOND SEMESTER B.Sc. DEGREE EXAMINATION, MARCH 2012

(CCSS)

Statistics—Complementary Course

ST 2C 02—PROBABILITY DISTRIBUTION

Time : Three Hours

Maximum : 30 Weightage

I. Answer *all* 12 questions1 The joint cumulative distribution function $F(x, y)$ lies within the limits.

- (a) —1 and 1. (b) —1 and 0.
 (c) $-\infty$ and $+\infty$. (d) 0 and 1.

2 $P\{X \leq a, Y \leq b\} = P\{X < a, Y < b\}$ provided.

- (a) X and Y are discrete random variables.
 (b) X and Y are continuous random variables.
 (c) X and Y are independent random variables.
 (d) X and Y are dependent random variables.

3 If X and Y are independent random variables, then

- (a) $P\{X \leq x, Y \leq y\} = P\{X \leq x\} \cdot P\{Y \leq y\}$
 (b) $E(XY) = E(X) \cdot E(Y)$.

(d) All the above.

4 The (1,1) product moment μ_{11} of a bivariate distribution is called.

- (a) Coefficient of Correlation. (b) Coefficient of determination.
 (c) Covariance. (d) None of these.

5 $E\{E(NY)\} =$

- (a) Zero. (b) one.
 (d) $E(X)$.

6 If X and Y are independent binomial $B\left(\quad\right)$ variates, then $Z = X + Y$ follows

(a) $B\left(6, \frac{1}{2}\right)$.

(b) $B\left(3, \frac{1}{2}\right)$.

(c) $BI\left(6, \frac{1}{4}\right)$.

(d) $B\left(3, \frac{1}{4}\right)$.

7 Variance of a discrete uniform distribution over the range [1, 11] is :

(a) 3.

(b) 6.

(c) 10. _____

(d) None of these.

8 If X has density $f(x) = \lambda e^{-\lambda x}$, $x > 0, \lambda > 0$, then $E(X)$ is

(a) λ^2

(b) $\frac{1}{\lambda^2}$.

(c) 2λ .

(d) $\frac{2}{\lambda^2}$.

9 Gamma distribution G(a) is :

(a) Leptokurtic.

(b) Mesokurtic.

(c) Platykurtic.

(d) Leptokurtic when $a > 1$.

10 If X_1 and X_2 are independent standard normal variates, $E(X_1 - X_2)^2$ is

(a) 0.5.

(b) 0.

(c) 1.

(d) 2.

11 If X is a standard normal variate, the value of t for which $P\{|X| > t\} = 0.05$ is

(a) 1.645.

(b) 1.96.

(c) 1.98.

(d) 2.34.

12 The income of people exceeding a certain limit follows :

(a) Cauchy.

(b) Lognormal.

(c) Pareto.

(d) Beta.

II. Short answer type questions. Answer all 9 questions.

13 Define cumulative distribution function of a bivariate random vector (X, Y).

14 Define conditional probability density function of Y given X.

15 Define conditional expectation in discrete case.

16 Define mathematical expectation of a bivariate random vector.

17 State the lack of memory property of geometric distribution.

18 Find the moment generating function of a degenerate distribution.

19 Define standard exponential distribution.

20 State the additive property of gamma distribution.

21 Define Pareto distribution.

(9 x 1 = 9 weightage)

III. Short essay or paragraph questions. Answer any five questions.

22 Let $f(x, y) = \begin{cases} 2, & 0 < x < 1; 0 < y < x \\ 0, & \text{otherwise,} \end{cases}$

check whether X and Y are independent.

23 For a distribution with joint probability density function

$$f(x, y) = \begin{cases} x e^{-(x+y)}, & x > 0; y \geq 0 \\ 0, & \text{elsewhere,} \end{cases}$$

Find E (Y) and E (XY).

24 Obtain an expression for variance of a random variable X in terms of conditional variance.

25 Derive the moment generating function of a rectangular distribution over $[-a, a]$. Hence obtain its variance.

26 Obtain the mode of a Poisson distribution.

27 Derive an expression for mean deviation about mean of normal distribution.

28 For a distribution with probability mass function $p(x) = 2^{-x}, x = 1, 2, \dots$, Obtain a lower bound to the probability $p\{|X - 2| \geq 2\}$, by using Chebychev's inequality.

(5 x 2 = 10 weightage)

N. Essay questions. Answer any *two* questions.

29 Three coins are tossed. Let X denote the number of heads on the first two coins and Y denote the number of heads on the last two : Find (i) $E(Y|X = 1)$ and (ii) Correlation coefficient between X and Y .

30 (a) State and establish **Renovsky** formula.

(b) Explain important properties and applications of normal distribution.

31 (a) State **Bienayme-Chebychev's** inequality.

(b) State and prove **Lindberg-Levy** form of CU.

(2 x 4 = 8 **weightage**)