

**FIFTH SEMESTER B.Sc. DEGREE (SUPPLEMENTARY) EXAMINATION
NOVEMBER 2017**

(UG—CCSS)

MM 5B 07—BASIC MATHEMATICAL ANALYSIS

Time : Three Hours

Maximum : 30 Weightage

Part A*Answer all questions.*

1. Define bijection.
2. Give an example of a denumerable set.
3. Give an example of a bounded below set which is not bounded above.
4. State nested interval property.
5. Is the sequence (n) convergent ?
6. Give an example of an unbounded sequence that has a convergent subsequence.
7. If (x_n) is an unbounded increasing sequence find $\lim x_n$.
8. Given an example of an open set which is not an interval.
9. Define Cantor set.
10. State Cauchy convergence criterion.
11. If z is real show that $z = \bar{z}$.
12. State de Moivre's formula.

(12 × ¼ = 3 weightage)

Part B*Answer all questions.*

13. By Mathematical Induction, prove that $1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$.
14. Determine the set $A = \{x \in \mathbb{R} \mid 2x + 3 < 7\}$.
15. Show that $\lim (1/n) = 0$.

Turn over

16. Prove that a convergent sequence of real numbers is bounded.
17. Give an example of a bounded sequence that is not a Cauchy sequence.
18. Show that the set of Natural numbers is a closed set.
19. Show that $\overline{iz} = -i\overline{z}$.
20. Find $(\text{Arg } z_1 z_2)$.
21. If $z_1 = 2i, z_2 = \frac{2}{3} - i$, find $z_1 + z_2$.

(9 × 1 = 9 weightage)

Part C

Answer any five questions.

22. Determine the set of all real numbers x such that $2x + 3 < 6$.
23. Find the infimum and supremum of $\left\{ \frac{1}{n} - \frac{1}{m} ; n, m \in \mathbb{N} \right\}$.
24. Find $\lim n^{1/n}$.
25. Is a Cauchy sequence of real numbers bounded ?
26. Show that a convergent sequence of real numbers is Cauchy.
27. Sketch the set of points determined by $|z + i| \leq 3$.
28. Prove that $\cos 3\theta = \cos^3 \theta - 3 \cos \theta \sin^2 \theta$.

(5 × 2 = 10 weightage)

Part D

Answer any two questions.

29. Prove that there exists a positive real number x such that $x^2 = 2$.
30. State and prove Bolzano Weierstrass Theorem.
31. Find the exponential form of the complex number $-1 - i, \frac{-1 + \sqrt{3}i}{2}$.

(2 × 4 = 8 weightage)